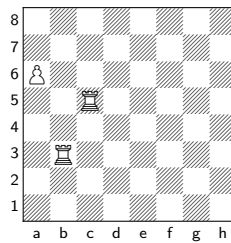


How many distinct  $n \times n$  chessboard are there with two white rooks and a pawn all occupying different rows and columns? Justify your answer.



**Solution:** If the white rooks were distinct the number of possible configurations can be counted using the product rule: There are  $n$  choices for the first rook's rows and columns,  $n - 1$  remaining for the second one, and  $n - 2$  remaining for the pawn's, giving a total of  $n \cdot n \cdot (n - 1) \cdot (n - 1) \cdot (n - 2) \cdot (n - 2) = (n \cdot (n - 1) \cdot (n - 2))^2$ .

Each actual configuration with indistinguishable white rooks arises from two configurations with distinct (labeled) white rooks. By the division rule, the desired number of configurations is  $(n \cdot (n - 1) \cdot (n - 2))^2 / 2$ .