- 1. Calculate the following numbers.
 - (a) $1 4 + 7 11 \mod 6$
 - (b) $11 \cdot 13 4 \cdot 5 \mod 17$
 - (c) $4 \cdot 9^{-1} \mod 23$
- 2. Calculate the following numbers using the suggested method:
 - (a) 2⁹ mod 11 using iterated multiplication.
 - (b) $2^{81} \mod 11$ using fast exponentiation (the *Power* algorithm from Lecture 5).
 - (c) $2^{2^{81}}$ mod 11 using Fermat's Little Theorem (Theorem 5 from Lecture 5).
- 3. Calculate the following numbers.
 - (a) x and y that solve $5x + 7y \equiv 17 \pmod{19}$ and $4x + 11y \equiv 13 \pmod{19}$.
 - (b) $1^1 + 2^2 + \dots + 99^{99} \mod 3$.
 - (c) (Optional) 42! mod 43 (*Hint:* Pair up each number with its inverse. You can try 6! mod 7 first.)
- 4. You will investigate the "baby RSA" encryption from Lecture 5. Recall that the public encryption key e and "secret" decryption key d are chosen so that $ed \equiv 1 \pmod{n-1}$ for prime modulus n.
 - (a) Assume n = 29 and d = 11. Show how to choose e to enable decryption.
 - (b) Calculate the encryption $c = m^e \mod n$ of the message m = 10 and the encryption key e from part (a). Then calculate the decryption $c^d \mod n$.
 - (c) Now suppose Eve observes the ciphertext c=33 that Alice sent to Bob using modulus n=37 and encryption key e=7. How can Eve recover the message m without knowing d?