- 1. The PDF of the random variable X is  $f(x) = Ce^{-|x|}$ , where x ranges over all real numbers. Determine (a) the value of C, (b) the CDF  $P(X \le x)$ , and (c) the probability that  $|X| \le 1$ .
- 2. The joint PDF of (X, Y) is

$$f_{X,Y}(x,y) = \begin{cases} C(x+y+1)y, & \text{if } 0 \le x \le 2, 0 \le y \le 2, \\ 0, & \text{otherwise.} \end{cases}$$

Find (a) the value of C and (b) The conditional PDF  $f_{Y|X}(y|x)$ .

- 3. Let X be a Uniform(0, 1) random variable. Find the PDF of the random variables (a)  $Y = e^X$  and (b)  $Z = -2 \log X$ .
- 4. Raindrops hit your head at a rate of 1 per second. What is the PDF of the time at which the second raindrop hits you? How about the third one? (**Hint:** convolution)
- 5. You draw 10 balls at random among 15 red and 5 blue balls without replacement. Let X be the number of red balls drawn.
  - (a) What is the expected value of X?
  - (b) Write  $X = X_1 + X_2 + \cdots + X_{10}$ , where  $X_i$  indicates if the *i*-th drawn ball is red. What is the variance of  $X_i$ ?
  - (c) What is the covariance of  $X_i$  and  $X_j$   $(i \neq j)$ ?
  - (d) What is the variance of X?